# General Certificate of Education (A-level) June 2012 

## Mathematics

MM04

## (Specification 6360)

Mechanics 4

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## Key to mark scheme abbreviations

| M | mark is for method |
| :--- | :--- |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0) accuracy marks |
| $-x$ EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

MM04

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | $M=\left(\frac{4-2}{2}, \frac{-1+1}{2}, \frac{4+6}{2}\right)=(1,0,5)$ | B1 |  | mid-point found |
|  | $\overrightarrow{P M}=-\left(\begin{array}{c} -2 \\ -1 \\ 4 \end{array}\right)+\left(\begin{array}{l} 1 \\ 0 \\ 5 \end{array}\right)=\left(\begin{array}{l} 3 \\ 1 \\ 1 \end{array}\right)$ | B1 | 2 | AG |
|  | alternative $\overrightarrow{P Q}=\left(\begin{array}{l} 4 \\ 1 \\ 6 \end{array}\right)-\left(\begin{array}{c} -2 \\ -1 \\ 4 \end{array}\right)=\left(\begin{array}{l} 6 \\ 2 \\ 2 \end{array}\right)$ | (B1) |  |  |
|  | $\overrightarrow{P M}=\frac{1}{2}\left(\begin{array}{l} 6 \\ 2 \\ 2 \end{array}\right)=\left(\begin{array}{l} 3 \\ 1 \\ 1 \end{array}\right)$ | (B1) | (2) | AG |
| (b) | $\begin{aligned} \text { Moment } & =\mathbf{r} \times \mathbf{F} \\ & =\left\|\begin{array}{ccc} \mathbf{i} & 3 & a \\ \mathbf{j} & 1 & 1 \\ \mathbf{k} & 1 & -2 \end{array}\right\| \end{aligned}$ | M1 |  | attempt at $\mathbf{r} \times \mathbf{F}$ or $\mathbf{F} \times \mathbf{r}$ |
|  | $=\left(\begin{array}{c} -3 \\ a+6 \\ 3-a \end{array}\right)$ | A2,1 | 3 | $\begin{aligned} & \text { one component correct } \Rightarrow \text { A1 } \\ & \mathbf{F} \times \mathbf{r} \text { attempt } \Rightarrow \text { M1A1A0 } \end{aligned}$ |
| (c) | Magnitude $=\sqrt{(-3)^{2}+(a+6)^{2}+(3-a)^{2}}$ | M1 |  | attempt at magnitude of their moment |
|  | Hence $9+(a+6)^{2}+(3-a)^{2}=50$ | A1F |  |  |
|  | $\begin{aligned} & a^{2}+3 a+2=0 \\ & (a+2)(a+1)=0 \end{aligned}$ | m1 |  | attempts to solve a quadratic - real roots |
|  |  | A1 | 4 | both values obtained; CAO <br> No further penalty for $\mathbf{F} \times \mathbf{r}$ attempt which is correct <br> ie $(3,-a-6, a-3)$ as components |
|  | Total |  | 9 |  |



MM04 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | $\binom{-2}{0}+\binom{0}{-5}+\binom{p}{1}+\binom{-3}{-4}=\binom{p-5}{-8}$ | B1 | 1 |  |
| (b)(i) | $\begin{aligned} & \text { Parallel to } y \text {-axis } \Rightarrow p-5=0 \\ & p=5 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | set $\mathbf{i}$ component $=0$ (seen or implied) |
| (ii) |  |  |  |  |
|  | Moments about $O$ for given system $\begin{aligned} & -5(4)+2(3)+3 q+5(2)-1(8) \\ & =3 q-12 \end{aligned}$ | M1 <br> A2,1F |  | $\begin{aligned} & \mathrm{F} \times \mathrm{d} \text { for at least four components } \\ & -1 \text { each type of error, } \mathrm{ft}(\mathrm{a}),(\mathrm{b})(\mathrm{i}) \\ & (12-3 q \text { scores M1A2) } \end{aligned}$ |
|  | Moments about $O$ for equivalent system $\begin{aligned} & =-8(3) \\ & =-24 \end{aligned}$ | B1 |  | $\pm 24 \text { seen }$ <br> ft ( a) allow $\pm 3 \times$ their $\mathbf{j}$ component |
|  | Hence $3 q-12=-24$ $3 q=-12$ | M1 |  | attempt at moment equation - must see clear use of Force $\times$ distance on RHS |
|  |  | A1F | 6 | ft error with $p$ from (b)(i) |
| (c) | $\|C\|=24$ | B1F |  | Should match part (b) - must be positive |
|  |  | B1 | 2 | accept 'clockwise' |
|  | Total |  | 11 |  |



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| :---: | :---: | :---: | :---: | :---: |
| 4(c) | Alternative 1 |  |  |  |
|  | $\begin{aligned} \text { PE before motion } & =m g l+4 m g(2 l) \\ & =9 m g l \end{aligned}$ | $\begin{gathered} (\mathrm{M} 1) \\ (\mathrm{A} 1) \end{gathered}$ |  | $m g h$ used total PE correct |
|  | $\begin{aligned} & \text { PE after motion } \\ & \qquad \begin{aligned} & =-3 m g l-m g l-4 m g l+3 m g l \\ & =-5 m g l \end{aligned} \\ & \text { KE before } \end{aligned}$ | (A1) |  | total PE correct |
|  | $\mathrm{KE} \text { after }=\frac{43}{3} m l^{2} \dot{\theta}^{2}$ | (B1F) |  | use of KE formula with MI from (b) |
|  | $\mathrm{C} \text { of } \mathrm{E} \Rightarrow 9 m g l=\frac{43}{3} m l^{2} \dot{\theta}^{2}-5 m g l$ | (M1) |  | attempt at C of E equation |
|  | $\Rightarrow \frac{43}{3} m l^{2} \dot{\theta}^{2}=14 m g l$ | (A1) |  | correct equation |
|  | $\Rightarrow \dot{\theta}=\sqrt{\frac{42 g}{43 l}}$ | (A1F) | (7) |  |
|  | Alternative 2 |  |  |  |
|  | Centre of mass of system at $\left(\frac{17}{12} l, \frac{3}{4} l\right)$ | (M1) |  | Centre of mass attempted |
|  | Change in height of centre of mass $=$ $\frac{3}{4} l+\left(\frac{17}{12} l-l\right)=\frac{7}{6} l$ | (A1) |  | Change in height seen/used |
|  | Total PE loss $=12 m g\left(\frac{7}{6} l\right)=14 m g l$ | $\begin{aligned} & \text { (A1) } \\ & \text { (A1) } \end{aligned}$ |  | $m g h$ used <br> Total loss found |
|  | $\mathrm{KE} \text { gain }=\frac{43}{3} m l^{2} \dot{\theta}^{2}$ | (B1F) |  | use of KE formula with MI from (b) |
|  | $\mathrm{C} \text { of } \mathrm{E} \Rightarrow \frac{43}{3} m l^{2} \dot{\theta}^{2}=14 m g l$ | (M1) |  | $C$ of $E$ equation formed |
|  | $\dot{\theta}=\sqrt{\frac{42 g}{43 l}}$ | (A1F) | (7) |  |



MM04 (cont)


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[^0]:    Further copies of this Mark Scheme are available from: aqa.org.uk

